## **Example 1:** Simplify.

a. 
$$(1 + \sin\theta)(1 - \sin\theta)$$

b. 
$$(5 + 5\cos\beta)(5 - 5\cos\beta)$$

c. 
$$(1 + \cot \omega)^2 - 2\cot \omega$$

## **Example 2:** Write the expression as a single fraction in terms of sine and cosine.

$$tan \gamma + \cot \gamma$$

## **Example 3**: Perform the addition and simplify.

$$\frac{1}{1+\sin v} + \frac{1}{1-\sin v}$$

**Example 4:** Rewrite  $\frac{\cos^2 y}{1-\sin y}$  so that it is *not* in fractional form.

**Example 5:** Use the substitution  $x = 5\sin\vartheta$ ,  $0 < \vartheta < \frac{\pi}{2}$  to write  $\sqrt{25 - x^2}$  as a trigonometric function of  $\vartheta$ .

## Lesson 5.1 Day 3 Worksheet

Date: \_\_\_\_\_ Hour: \_\_\_\_

Perform each indicated operation and simplify the result.

1. 
$$cot\theta + \frac{1}{cot\theta}$$

$$2. \frac{\sec x}{\csc x} + \frac{\csc x}{\sec x}$$

3. 
$$tan v (cot v + csc v)$$

4. 
$$\cos \gamma (\sec \gamma + \csc \gamma)$$

$$5. \frac{\cos\beta}{\sec\beta} + \frac{\sin\beta}{\csc\beta}$$

6. 
$$\frac{\cos\theta}{\sin\theta} + \frac{\sin\theta}{1+\cos\theta}$$

7. 
$$(2csc x + 2)(2csc x - 2)$$
 8.  $(sin b + cos b)^2$ 

8. 
$$(\sin b + \cos b)^2$$

9. 
$$(1 + \sin \alpha)^2 + \cos^2 \alpha$$

10. 
$$(1 + \tan r)^2 - 2\tan r$$
 11.  $\frac{1}{1 + \cos \beta} + \frac{1}{1 - \cos \beta}$ 

$$11. \ \frac{1}{1+\cos\beta} + \frac{1}{1-\cos\beta}$$

12. 
$$\frac{1}{\sec x + 1} + \frac{1}{\sec x - 1}$$

Factor each trigonometric expression.

13. 
$$2\sin^2 x + 3\sin x + 1$$

13. 
$$2\sin^2 x + 3\sin x + 1$$
 14.  $4\tan^2 \vartheta + \tan \vartheta - 3$  15.  $\sin^2 \omega - 1$ 

15. 
$$sin^2\omega - 1$$

Use identities to simplify each expression into a single expression.

17. 
$$\frac{\sin^2 x}{\cos^2 x} + \sin x \csc x$$

17. 
$$\frac{\sin^2 x}{\cos^2 x} + \sin x \csc x$$
 18. 
$$\frac{1}{\tan^2 \beta} + \cot \beta \tan \beta$$