Example 1: Simplify.
a. $(1+\sin \theta)(1-\sin \theta)$
b. $(5+5 \cos \beta)(5-5 \cos \beta)$
c. $(1+\cot \omega)^{2}-2 \cot \omega$

Example 2: Write the expression as a single fraction in terms of sine and cosine.
$\tan \gamma+\cot \gamma$

Example 3: $\quad$ Perform the addition and simplify.
$\frac{1}{1+\sin v}+\frac{1}{1-\sin v}$

Example 4: $\quad$ Rewrite $\frac{\cos ^{2} y}{1-\sin y}$ so that it is not in fractional form.

Example 5: $\quad$ Use the substitution $\mathrm{x}=5 \sin \vartheta, 0<\vartheta<\frac{\pi}{2}$ to write $\sqrt{25-x^{2}}$ as a trigonometric function of $\vartheta$.
$\qquad$
Date: $\qquad$ Hour: $\qquad$

Perform each indicated operation and simplify the result.

1. $\cot \theta+\frac{1}{\cot \theta}$
2. $\frac{\sec x}{\csc x}+\frac{\csc x}{\sec x}$
3. $\tan v(\cot v+\csc v)$
4. $\cos \gamma(\sec \gamma+\csc \gamma)$
5. $\frac{\cos \beta}{\sec \beta}+\frac{\sin \beta}{\csc \beta}$
6. $\frac{\cos \theta}{\sin \theta}+\frac{\sin \theta}{1+\cos \theta}$
7. $(2 \csc x+2)(2 \csc x-2)$
8. $(\sin b+\cos b)^{2}$
9. $(1+\sin \alpha)^{2}+\cos ^{2} \alpha$
10. $(1+\tan r)^{2}-2 \tan r$
11. $\frac{1}{1+\cos \beta}+\frac{1}{1-\cos \beta}$
12. $\frac{1}{\sec x+1}+\frac{1}{\sec x-1}$

Factor each trigonometric expression.
13. $2 \sin ^{2} x+3 \sin x+1$
14. $4 \tan ^{2} \vartheta+\tan \vartheta-3$
15. $\sin ^{2} \omega-1$

Use identities to simplify each expression into a single expression.
16. $\sec \gamma \cos \gamma$
17. $\frac{\sin ^{2} x}{\cos ^{2} x}+\sin x \csc x$
18. $\frac{1}{\tan ^{2} \beta}+\cot \beta \tan \beta$

