

**Review:** In a – d, express as a single logarithm.

a.  $2\log_x 4 - 3\log_x y$

b.  $4\log_k w + 2\log_k 9$

c.  $7\log_5 t + 3\log_5 k - 2\log_5 g$

d.  $\frac{4\log_3 k}{3}$

e. The formula for earthquake magnitude is  $M = \log \frac{x}{0.001}$  where  $x$  is the seismographic reading of the earth quake in mm. Express the formula in expanded form.

**Example 1:** Write each logarithm in terms of  $\ln 2$  and  $\ln 5$ .

a.  $\ln 10 =$

b.  $\ln \frac{25}{2} =$

**Example 2:** Use the properties of logarithms to rewrite and simplify the logarithmic expression.

a.  $\log_2 8 =$

b.  $\ln(5e^6) =$

**Example 3:** Find the exact value of each expression without using a calculator.

a.  $\log_3 9 =$

b.  $\log_7 \sqrt[5]{7} =$

c.  $\ln e^{12} + \ln e^5 =$

**Example 4:** Expand each Logarithmic Expression.

a.  $\log 3x^2y =$

b.  $\ln \frac{\sqrt{4x+1}}{8} =$

c.  $\log_2 xyz^3 =$

**Example 5:** Condense each Logarithmic Expression.

a.  $\frac{1}{3} \log x + 5 \log(x - 3)$

b.  $4 \ln(x - 4) - 2 \ln x$

c.  $\frac{1}{5} [\log_3 x + \log_3(x + 1)]$

**Example 6:** A pebble is dropped into a calm pond, causing ripples in the form of concentric circles. The table below gives the radius  $r$  and the area  $A$  of the outer ripple in feet. Find an equation that expresses  $A$  as a function of  $r$ .

$r$	0.6	1.2	1.8	2.4	3.0	3.6
$A$	1.131	4.524	10.179	18.096	28.274	40.715

**Step 1:** Rewrite the table by taking the natural log of each number.

$\ln r$						
$\ln A$						

**Step 2:** Find the slope

**Remember  $m$  is slope so in this case,**

$$m = \frac{\ln y_2 - \ln y_1}{\ln x_2 - \ln x_1}$$

**Step 3:** Write the equation.

Instead of using  $y = mx + b$ ,  
use  $\ln y = m \ln x + b$