Example 1: A. Graph the polar equation $r=2 \cos \vartheta$
B. Find the zeros and the maximum value of $r$ for the graph of $r=2 \cos \vartheta$..


| $\boldsymbol{\vartheta}$ | $\boldsymbol{r}$ |
| :---: | :---: |
| 0 | 2 |
| $\pi / 6$ | $\sqrt{3}$ |
| $\pi / 3$ | 1 |
| $\pi / 2$ | 0 |
| $\frac{2 \pi}{3}$ | -1 |
| $5 \pi / 6$ | $-\sqrt{3}$ |
| $\pi$ | -2 |
| $7 \pi / 6$ | $-\sqrt{3}$ |
| $3 \pi / 2$ | 0 |
| $11 \pi / 6$ | $\sqrt{3}$ |
| $2 \pi$ | 2 |

Example 2: Find the zeros and the maximum value of $r$ for the graph $r=-3 \sin \vartheta$.

## Tests for Symmetry in Polar Coordinates

| S.W.R.T. | Test | Example |
| :---: | :---: | :---: |
| The Line $\theta=\pi / 2$ | Replace $\qquad$ with $\qquad$ then use the sum/difference formulas |  |
| The Polar Axis | Replace $\qquad$ with $\qquad$ then use the even/odd identities. |  |
| The Pole | Replace $\qquad$ with $\qquad$ then simplify. |  |
| Sum and Difference Formulas: <br> $\sin (u \pm v)=\sin u \cos v \pm \cos u \sin v$ <br> $\cos (u \pm v)=\cos u \cos v \mp \sin u \sin v$ |  |  |

Even/Odd Identities: Sine, cosecant, tangent and cotangent are odd functions. Cosine and secant are even functions.

$$
\begin{array}{lll}
\sin (-\theta)=-\sin (\theta) & \cos (-\theta)=\cos (\theta) & \tan (-\theta)=-\tan (\theta) \\
\csc (-\theta)=-\csc (\theta) & \sec (-\theta)=\sec (\theta) & \cot (-\theta)=-\cot (\theta)
\end{array}
$$

## Example 3: Test the following polar equations for each type of symmetry.

a. $r=2 \cos \vartheta$
b. $r=\frac{3}{2+\sin \vartheta}$
c. $r^{2}=25 \sin 2 \vartheta$

