$\qquad$
$\qquad$ Hour Real Numbers and Their Properties

## The Real Number System



| Type | Definition | Examples |
| :---: | :---: | :---: |
| Natural | The set of numbers 1, 2, 3, 4, ... Also called the $\qquad$ numbers. | 1, 2, 3, 4, ... |
| Whole | Natural numbers (counting numbers) and | 0, 1, 2, 3, 4, .. |
| Integers | Whole numbers and their | $\ldots,-2,-1,0,1,2, \ldots$ |
| Rational | Any number that can be written as a $\qquad$ When in decimal form the number pattern repeats or terminates. | $\begin{aligned} & 3 / 4,-41 / 2,7.95, \\ & \text { and } 0.123123 \ldots \end{aligned}$ |
| Irrational | Numbers that $\qquad$ be expressed as a ratio of two integers. Their decimal expansions are nonending and nonrepeating. | $\pi, \sqrt{2}, \sqrt[3]{19}$ |
| Real | All __and | numbers. |
| A Quizlet link is available on Schoology to help you STUDY these definitions! |  |  |

Example 1: Name all sets of numbers to which each real number belongs. Circle the smallest set.
a. $-\frac{17}{31}$
b. 23
c. 0
d. 4.581
e. -12
h. $\sqrt{3}$

Example 2: Which set of number is most reasonable for the situation?
a. the number of M\&M candies in a bag
b. outdoor temperatures
c. an ingredient list for baking cookies
d. the area of a circle

# Properties of Real Numbers 

Let $\mathrm{a}, \mathrm{b}$, and c represent real numbers.

| Property | of Addition | of Multiplication |
| :--- | :---: | :---: |
| Closure | $\mathrm{a}+\mathrm{b}$ is a real number | ab is a real number |
| Commutative | $\mathrm{a}+\mathrm{b}=\mathrm{b}+\mathrm{a}$ | $\mathrm{ab}=\mathrm{ba}$ |
| Associative | $(\mathrm{a}+\mathrm{b})+\mathrm{c}=\mathrm{a}+(\mathrm{b}+\mathrm{c})$ | $(\mathrm{ab}) \mathrm{c}=\mathrm{a}(\mathrm{bc})$ |
| Identity | $\mathrm{a}+0=\mathrm{a}, 0+\mathrm{a}=\mathrm{a}$ | $\mathrm{a} \cdot 1=\mathrm{a}, 1 \cdot \mathrm{a}=\mathrm{a}$ |
| Inverse | $\mathrm{a}+(-\mathrm{a})=0$ | $\mathrm{a} \cdot \frac{1}{\mathrm{a}}=1, \mathrm{a} \neq 0$ |


| Other Properties |  |
| :--- | :---: |
| Distributive | $\mathrm{a}(\mathrm{b}+\mathrm{c})=\mathrm{ab}+\mathrm{ac}$ |
| Multiplication Property of Zero | $a \cdot 0=0$ |
| Multiplication Property of $\mathbf{- 1}$ | $-1 \cdot a=-a$ |

Example 3: Name the property of real numbers illustrated by each equation.
a. $6+-6=0$
b. $(-4 \cdot 1)-2=-4-2$
c. $t+0=t$
d. $(d \cdot 4) \cdot 3=d \cdot(4 \cdot 3)$
e. $\frac{2}{3} \cdot \frac{3}{2}=1$
f. $\sqrt{7} \cdot 2=2 \cdot \sqrt{7}$
g. $m \cdot 0=0$
h. $\sqrt{2}(\pi+7)=\pi \sqrt{2}+7 \sqrt{2}$
i. $1 m=m$
j. $(-3+4)+5=-3+(4+5)$
k. $3(8 \cdot 0)=(3 \cdot 8) 0$
I. $(3+0)-5=3-5$
m. $9+7=7+9$
n. $-q=-1 q$

Example 4: Use the distributive property to find each product.
a. $2(x+4)$
b. $-3(4 y-7)$
c. $-(x+4)$
d. $2 x(3 x-1)$

